



JET isotope studies and the L-H transition

Emilia R. Solano, JET L2H Team Emilia.Solano@ciemat.es

Laboratorio Nacional de Fusión, CIEMAT, Spain

Special thanks: C. Silva, G. Birkenmeier, E. Delabie

Work supported in part by Spanish National Plan for Scientific and Technical Research and Innovation 2017-2020, grant numbers FIS2017-85252-R and PID2021-127727OB-I00, funded by MCIN/AEI/10.13039/501100011033 and ERDF 'A way of making Europe'.



This work has been carried out within the framework of the EUROfusion Consortium, funded by the European Union via the Euratom Research and Training Programme (Grant Agreement No 101052200 — EUROfusion). Views and opinions expressed are however those of the author(s) only and do not necessarily reflect those of the European Union or the European Commission. Neither the European Union nor the European Commission can be held responsible for them.





E.R. Solano¹, E. Delabie², G. Birkenmeier^{3,4}, C. Silva⁵, J. Hillesheim⁶, P. Vincenzi⁷, A.H. Nielsen⁸, J.J. Rasmussen⁸, A. Baciero¹, S. Aleiferis^{6,9}, I. Balboa⁶, A. Boboc⁶, C. Bourdelle¹⁰, I.S. Carvalho⁵, P. Carvalho⁵, M. Chernyshova¹¹, R. Coelho⁵, T. Craciunescu¹², R. Dumont¹⁰, E. de la Luna¹, J. Flanagan⁶, M. Fontana¹³, J.M. Fontdecaba¹, L. Frassinetti¹⁴, D. Gallart¹⁵, J. Garcia¹⁰, E. Giovannozzi¹⁶, C. Giroud⁶, W. Gromelski¹¹, R. Henriques⁵, L. Horvath⁶, I. Jecu¹², A. Kappatou⁴, D.L. Keeling⁶, D. King⁶, E. Kowalska-Strzëciwilk¹¹, M. Lennholm¹⁷, E. L. Erche¹⁸, E. Litherland-Smith⁶, V. Kiptily⁶, K. Kirov⁶, A. Loarte¹⁹, B. Lomanowski²⁰, C.F. Maggi⁶, M.J. Mantsinen²¹, A. Manzanares²², M. Maslov⁶, A.G. Meigs⁶, R.B. Morales⁶, D. Nina⁵, C. Noble⁶, V. Parail⁶, F. Parra Diaz²³, E. Pawelec²⁴, G. Pucella¹⁶, D. Réfy²⁵, E. Righi-Steele¹⁷, F.G. Rimini⁶, T.R. Robinson⁶, S. Saarelma⁶, M. Sertoli⁶, A. Shaw⁶, S. Silburn⁶, P. Sirén⁶, Z. Stancar²⁶, H. Sun⁶, G. Szepesi⁶, D. Taylor⁶, E. Tholerus¹⁴, S. Vartanian¹⁰, G. Verdoolaege²⁷, B. Viola¹⁶, H. Weisen¹³, T. Wilson⁶ and JET Contributors**

EUROfusion Consortium, JET, Culham Science Centre, Abingdon, OX14 3DB, UK

¹Laboratorio Nacional de Fusión, CIEMAT, Madrid, Spain; ²Oak Ridge National Laboratory, Oak Ridge, United States of America; ³Physik-Department E28, Technische Universität München, Garching, Germany; ⁴Max-Planck-Institut für Plasmaphysik, Garching, Germany; ⁵Instituto de Plasmas e Fusão Nuclear, Instituto Superior Técnico, Universidade de Lisboa, Portugal; ⁶CCFE, Culham Science Centre, Abingdon, United Kingdom of Great Britain and Northern Ireland; ⁷Consorzio RFX, Padova, Italy; ⁸Department of Physics, Technical University of Denmark, Kgs Lyngby, Denmark; ⁹NCSR 'Demokritos' 153 10, Agia Paraskevi Attikis, Greece; ¹⁰CEA, IRFM, Saint Paul Lez Durance, France; ¹¹Institute of Plasma Physics and Laser Microfusion, Warsaw, Poland; ¹²The National Institute for Laser, Plasma and Radiation Physics, Magurele-Bucharest, Romania; ¹³Ecole Polytechnique Fédérale de Lausanne (EPFL), Lausanne, Switzerland; ¹⁴Fusion Plasma Physics, Stockholm, Sweden; ¹⁵Barcelona Supercomputing Center, Barcelona, Spain; ¹⁶Unità Tecnica Fusione, ENEA C. R. Frascati, Frascati (Roma), Italy; ¹⁷European Commission, B-1049 Brussels, Belgium; ¹⁸Laboratory for Plasma Physics Koninklijke Militaire School, Ecole Royale Militaire Renaissancelaan, Brussels, Belgium; ¹⁹ITER Organization, Saint Paul Lez Durance, France; ²⁰Aalto University, Aalto, Finland; ²¹ICREA and Barcelona Supercomputing Center, Barcelona, Spain; ²²Universidad Complutense de Madrid, Madrid, Spain; ²³Rudolf Peierls Centre for Theoretical Physics, University of Oxford, Oxford, United Kingdom of Great Britain and Northern Ireland; ²⁴Institute of Physics, Opole University, Opole, Poland; ²⁵Wigner Research Centre for Physics, Budapest, Hungary; ²⁶Slovenian Fusion Association (SFA), Jozef Stefan Institute, Ljubljana, Slovenia; ²⁷Department of Applied Physics, UG (Ghent University), Ghent, Belgium

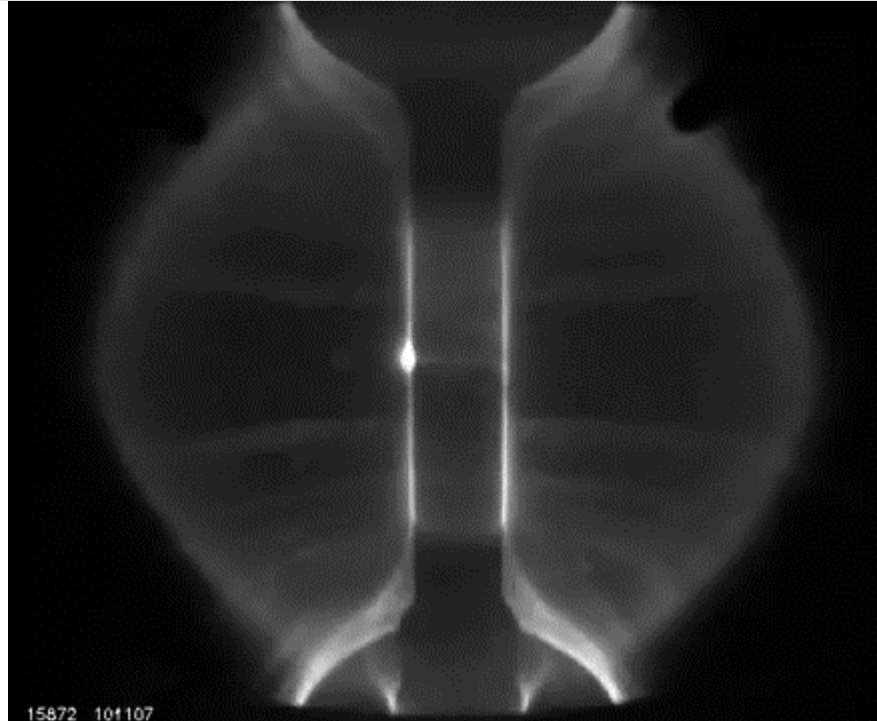
Acknowledgements: T. Estrada, C. Hidalgo, A. Alonso, D. Carralero, B. van Milligen

** See the author list of 'Overview of JET results for optimising ITER operation' by J. Mailloux et al to be published in Nuclear Fusion Special issue: Overview and Summary Papers from the 28th Fusion Energy Conference (Nice, France, 10-15 May 2021)



- Famous L-H transition movie from MAST
- Fusion, DT, JET
- L-H power threshold. P_{LH}
- P_{LH} scaling
- L-H time evolution, pedestal formation
- Minimum P_{LH} at $n_{e,min}$: isotope effect & critical profiles, A_{eff}
- ExB model vs. measurements: no evolution of v_{perp} along power ramp
- Alternate model: plasma magnetisation, motion of magnetised flux tubes

MAST Video of L-H transition



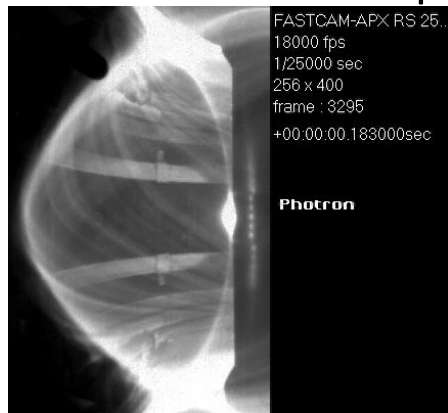
10 μ s exposure time
1 frame every 0.13 ms
(7.5 kHz)

A Kirk & MAST Team, Plasma Phys. Control. Fusion **48** (2006) B433–B441

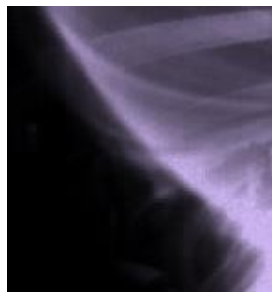
What do we see?



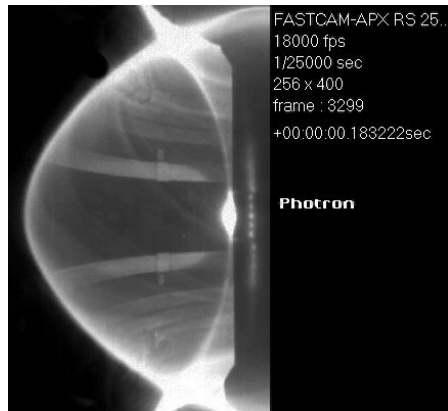
- Turbulence at the plasma edge disappears



L-mode: the edge looks diffuse, there are spinning plasma filaments that drift outside the separatrix, leading to losses



In $\sim 100 \mu\text{s}$. 1-2 frames:
L-H transition



H mode: the edge is sharp, no filaments or turbulence reach across the separatrix

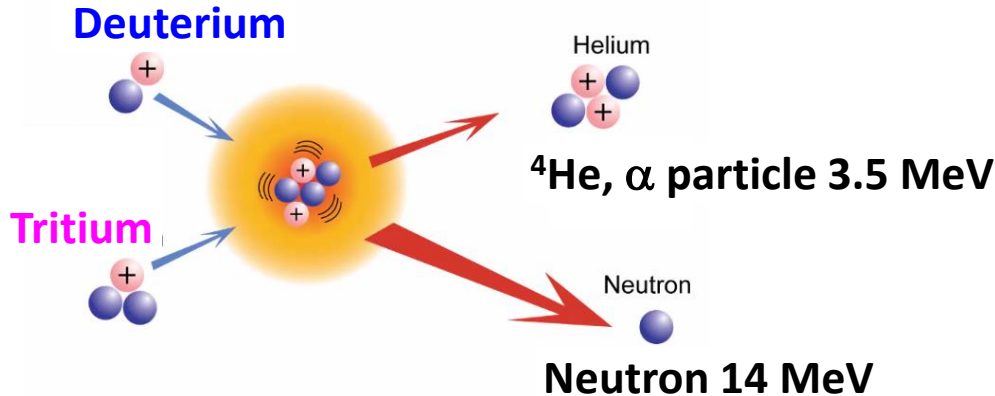


Isotopes of Hydrogen

Isotopes, Mix	A, A _{eff}	Plasma confinement	Wall interaction
Hydrogen	1 ●	Poor	Low
Deuterium	2 ■	Medium	Medium
DT 50/50	2.5 ★	Good	Acceptable?
Tritium	3 ◆	Very good	Not always

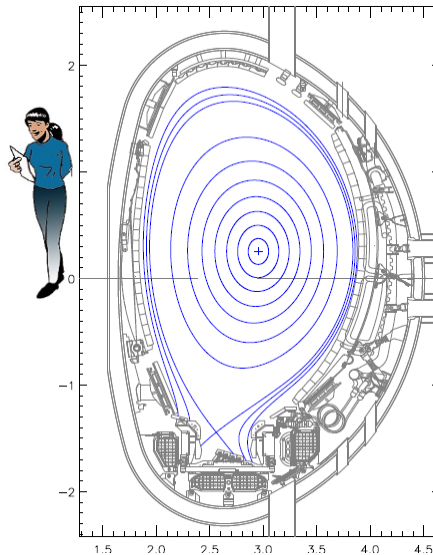
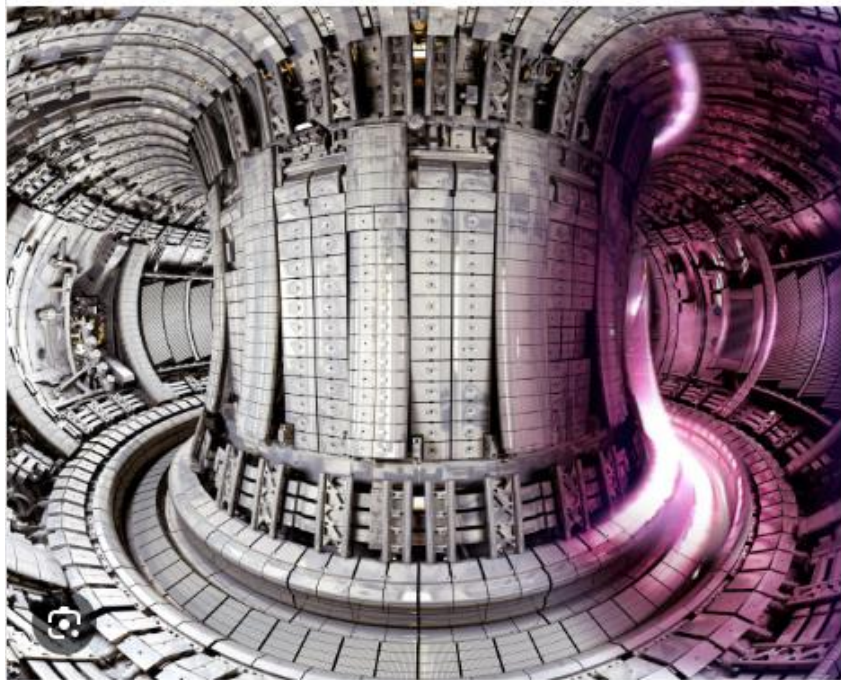
Confinement:

$$\tau_E = \frac{W_{\text{plasma}}}{P_{\text{heat}}} = \frac{\text{Plasma energy}}{\text{Input power}}$$



Ideally $T_{\text{ion}} > 10$ kV for optimal DT fusion cross-section

The JET tokamak: Hydrogen, Deuterium, Tritium, DT plasmas



JET Tokamak

Plasma characteristics:

$$R = 3 \text{ m}, a = 1 \text{ m}$$

$$\text{Volume} = 80 \text{ m}^3$$

$$I_p \leq 4 \text{ MA}$$

$$B_{\text{tor}} \leq 4 \text{ T}$$

JET is large!

Unique Tritium and Deuterium-Tritium capability

Stopped end 2023, breaking fusion records

Could be re-started if funding found

JET-ILW: W divertor, Be walls

Vacuum vessel 4.6 m high x 9 m wide

Power threshold to reach H-mode



- Discovery of H-mode: [F. Wagner Phys. Rev. Lett. 49, 1408 \(1982\)](#)
- Experiments show that, for otherwise fixed plasma conditions, there is a power threshold to enter H-mode.
- Predicting the appearance of H-mode for future devices requires understanding the power threshold
- In the absence of understanding for L-H transition trigger conditions, experiments with slow power ramps provide measurements of P_{LH}
- Multi-machine scaling studies are used to investigate dependencies of the power threshold.
- Plasma composition affects the power threshold
- Tokamak size, field, current, plasma shape: all affect P_{LH}

Multi-machine P_{LH} databases, scaling



The power required to achieve L-H is measured as:

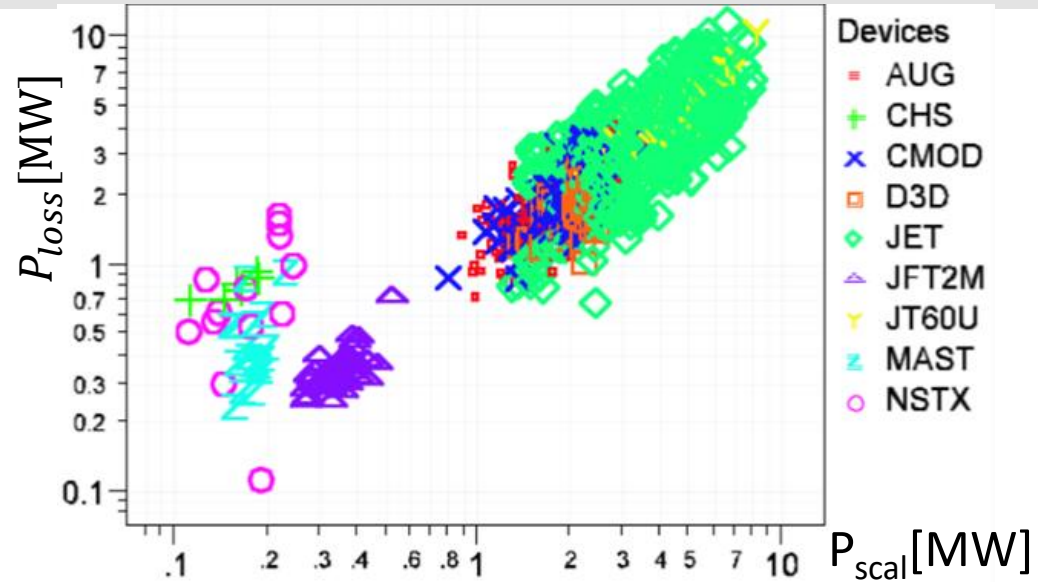
$$P_{loss} = P_{Ohm} + P_{aux} - dW/dt - P_{Fa_{stLoss}}$$

Depending on circumstances and data availability it may be useful to discount bulk radiated power ($\Psi_N < 0.95$)

$$P_{sep} = P_{loss} - P_{rad,bulk}$$

ITPA 2008 P_{LH} multimachine scaling, derived for Deuterium, single null, no ECRH heating (quite old).

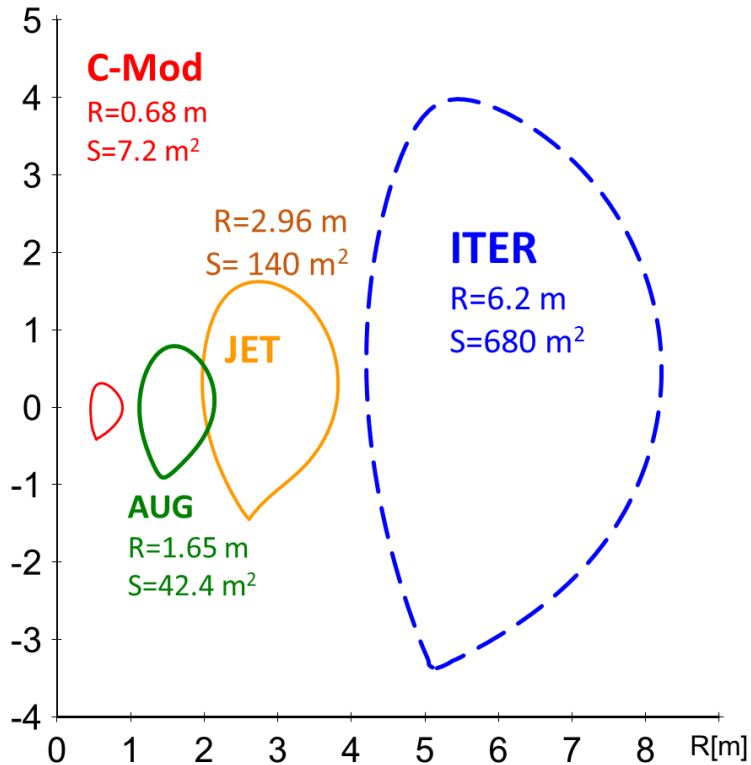
[Martin J. Phys. Conf. Ser. 123 012033 \(2008\)](#)



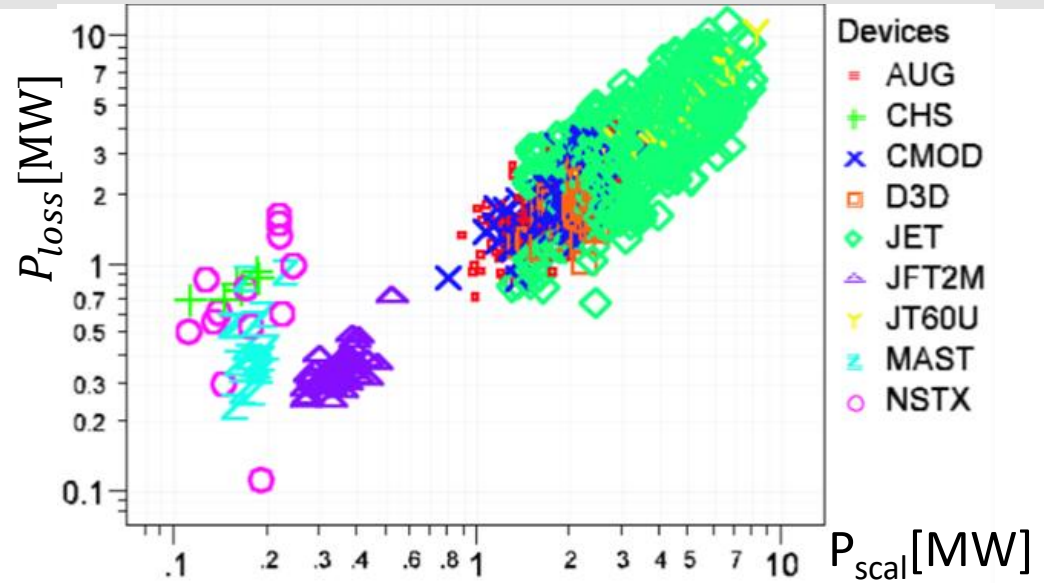
$$P_{scaling} = 0.049 n_{e20}^{0.72 \pm 0.03} B_T^{0.83 \pm 0.03} S^{0.94 \pm 0.02} (2/A)$$

- S is plasma surface area
- n_{e20} average electron density
- n_e , I_p and B_t are colinear in most studies
- **A** represents effective ion mass

Multi-machine P_{LH} databases, scaling



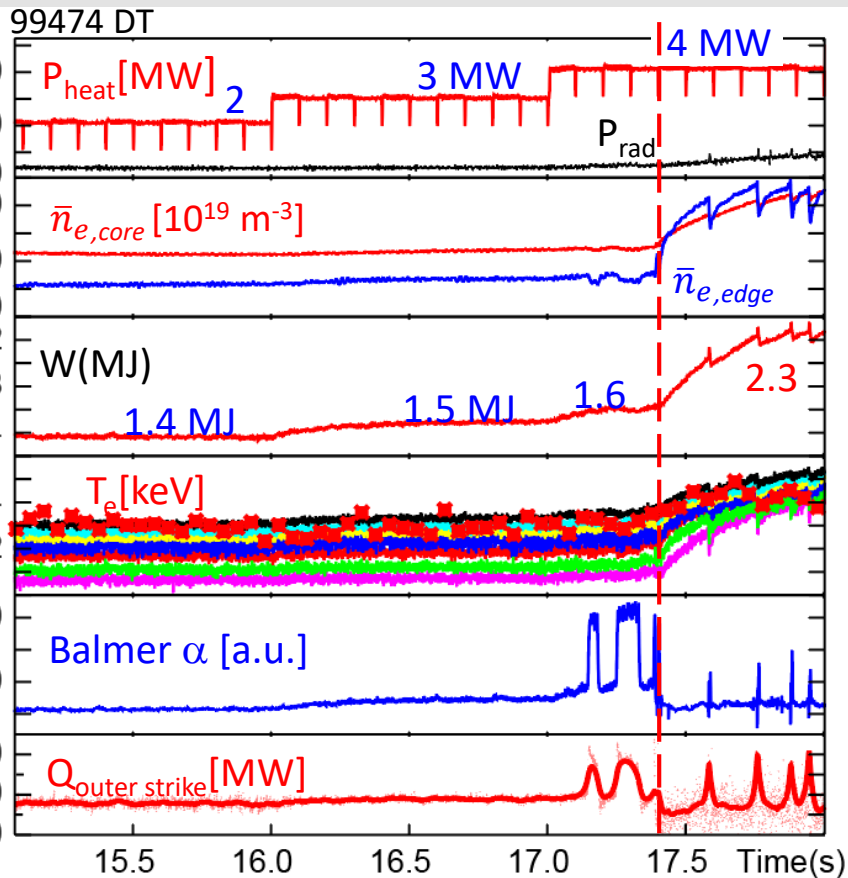
Metal wall makes a difference



$$P_{\text{scaling}} = 0.049 n_{e20}^{0.72 \pm 0.03} B_T^{0.83 \pm 0.03} S^{0.94 \pm 0.02} (2/A)$$

Work in progress: metal wall multi/machine scaling,
 Including new data from AUG, JET, C-Mod

L-H transition: from Low to High confinement (H-mode)



Experiment with constant gas

In L-mode

2 MW NBI: 1.4 MJ

3 MW NBI: 1.5 MJ

4 MW NBI: 1.6 MJ

L-H transition: 1.66 MJ

H-mode:

4 MW NBI: 2.3 MJ

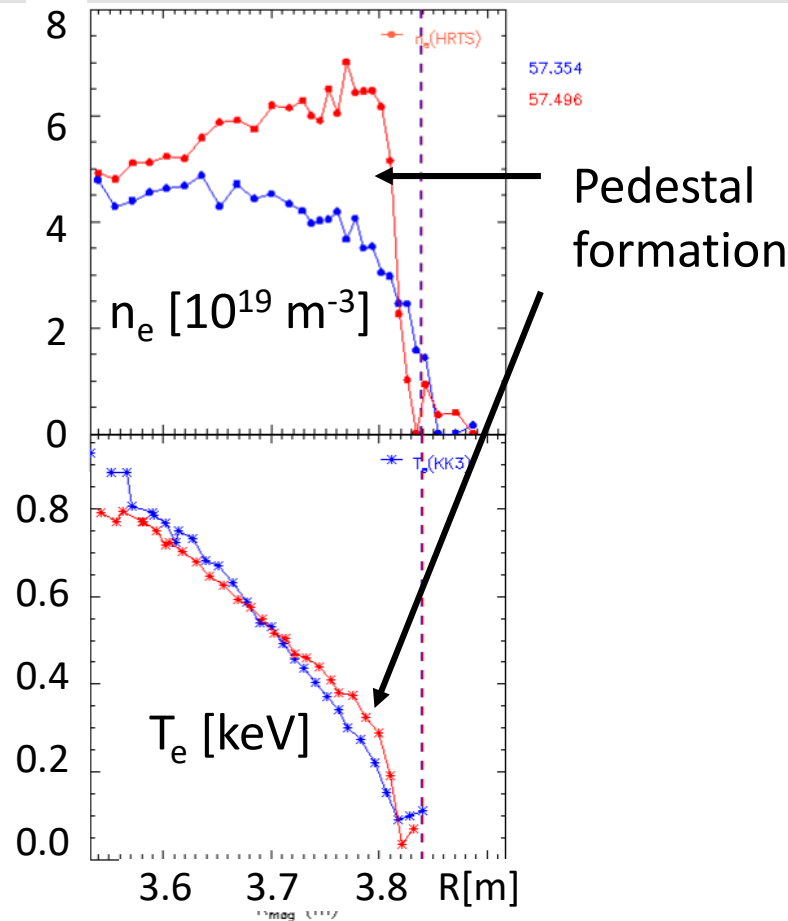
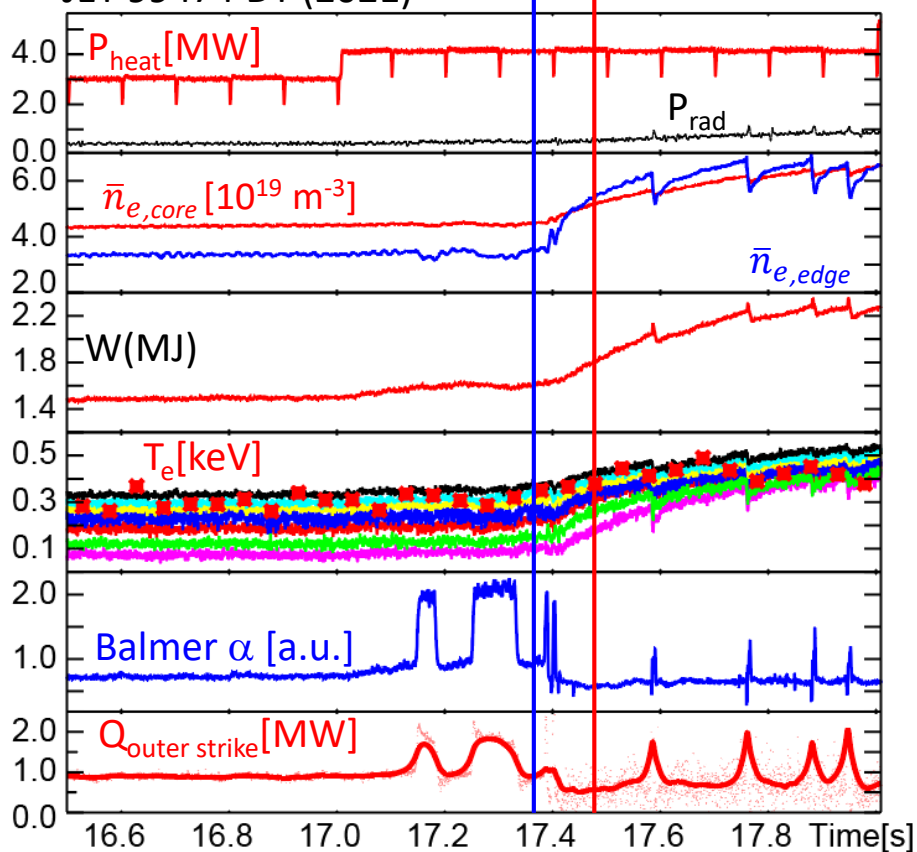
...

L-H transition allows the plasma to keep heat and particles in

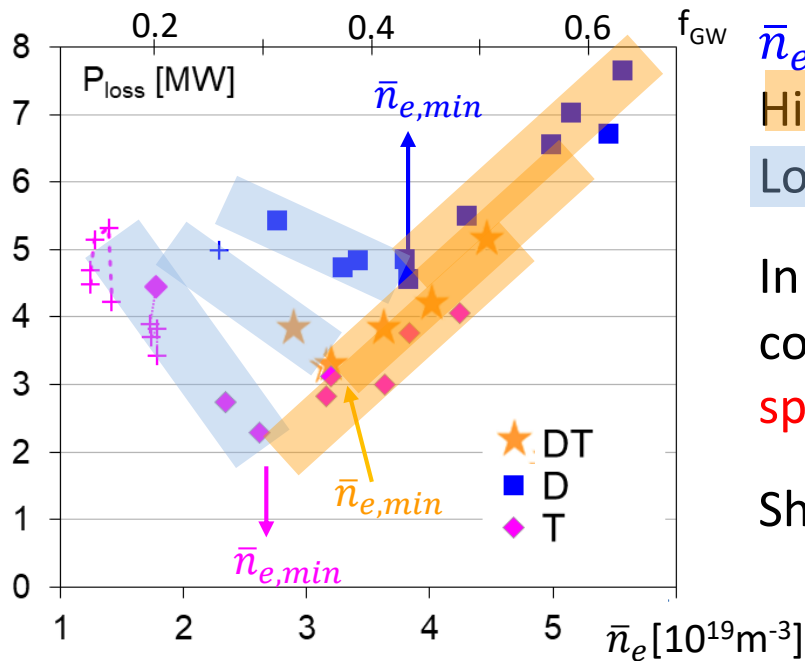
L-H transition: from Low to High confinement (H-mode)



JET 99474 DT (2021)



JET 3T, 2.5 MA: $\bar{n}_{e,min}$, $P_{LH,min}$, high and low ne branches



$\bar{n}_{e,min}$ is density at which P_{LH} is lowest, $P_{LH,min}$

High density branch: $\bar{n}_e > \bar{n}_{e,min}$

Low density branch: $\bar{n}_e < \bar{n}_{e,min}$

In JET $\bar{n}_{e,min}$ depends on plasma and divertor configuration/shape, divertor material, plasma species and plasma current.

Shift of $\bar{n}_{e,min}$ with isotope clearest in JET

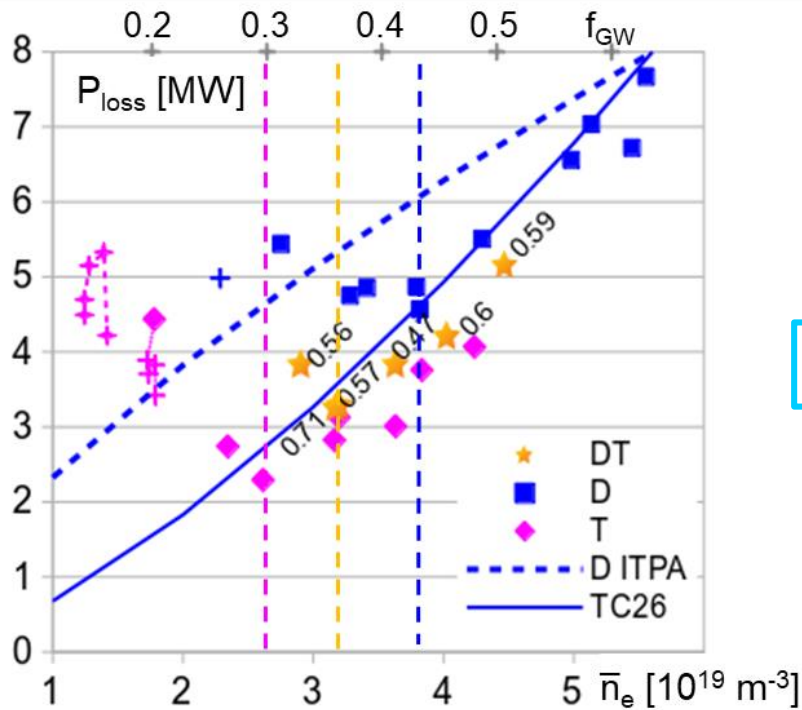
Clear shift of $\bar{n}_{e,min}$: lowest for T, then DT, then D.

E.R. Solano et al., Nucl. Fusion 63 (2023) 112011

<https://doi.org/10.1088/1741-4326/acee12>



P_{LH} in 3T 2.5 MA dataset



Potential easier access to H-mode in T-rich plasmas at lower density, to be evaluated vs. T consumption for ITER, DEMO, SPARC?

ITPA 2008 scaling doesn't match D data

$$P_{ITPA} = 0.049 n_{e20}^{0.72 \pm 0.03} B_T^{0.83 \pm 0.03} S^{0.94 \pm 0.02} (2/A)$$

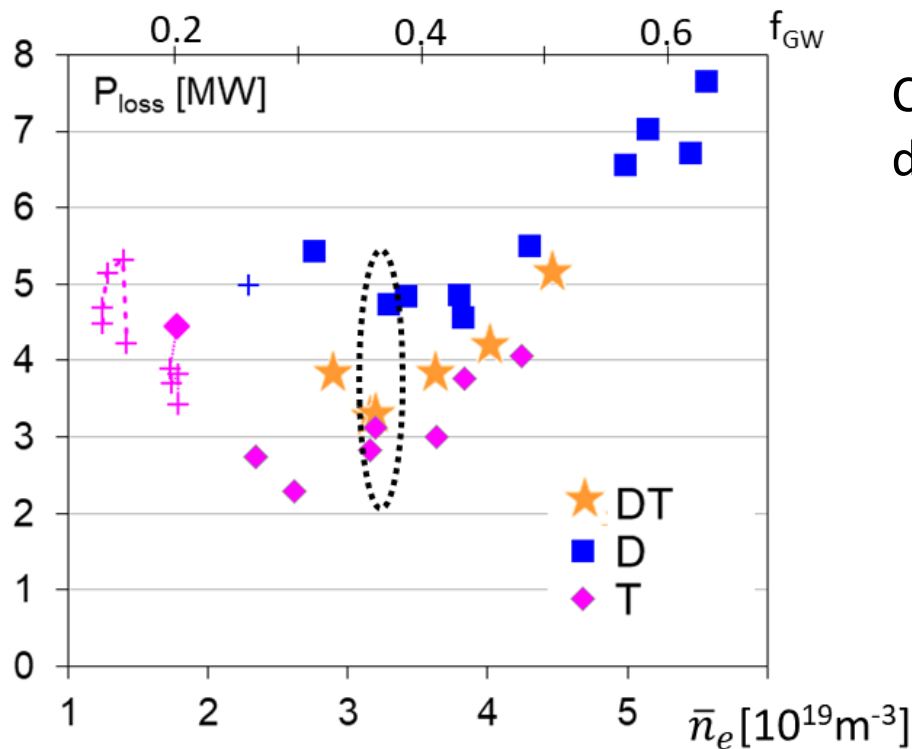
New JET scaling proposed, stronger dependency on n_e

$$P_{TC26-iso} = 0.057 \bar{n}_{e20}^{1.43} B_{tor}^{0.77} S (2/A_{eff})$$

Work ongoing:

multimachine metal P_{LH} scaling, including new JET data (E Delabie, APS 2024)

Critical profiles at L-H transition

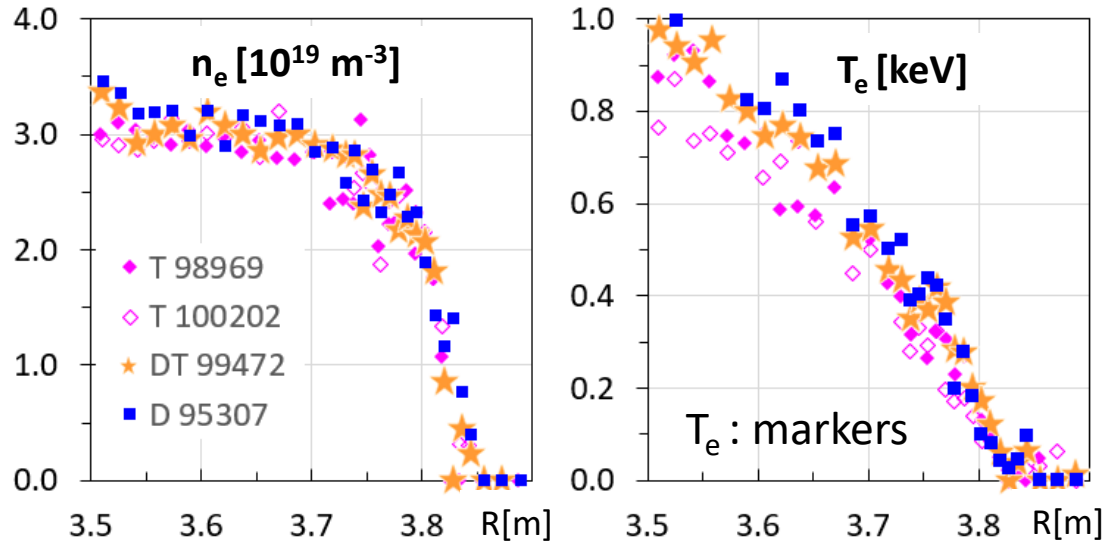


Compare profiles at transition for different species, at given density

3T 2.5 MA critical profiles



Thomson Scattering < 50 ms before L-H



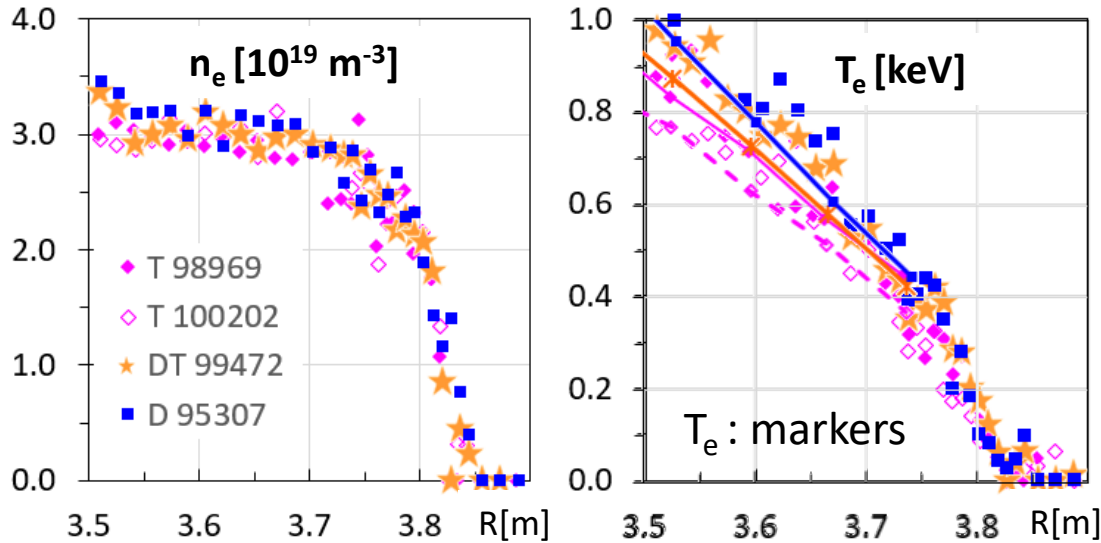
From $r/a=0.5$, very similar n_e , T_e , T_i profiles just before the transition in **D**, **DT**, **T**

ER Solano IAEA FEC 2023

3T 2.5 MA critical profiles



Thomson Scattering < 50 ms before L-H



$T_i \sim T_e$ (solid lines), Core CX

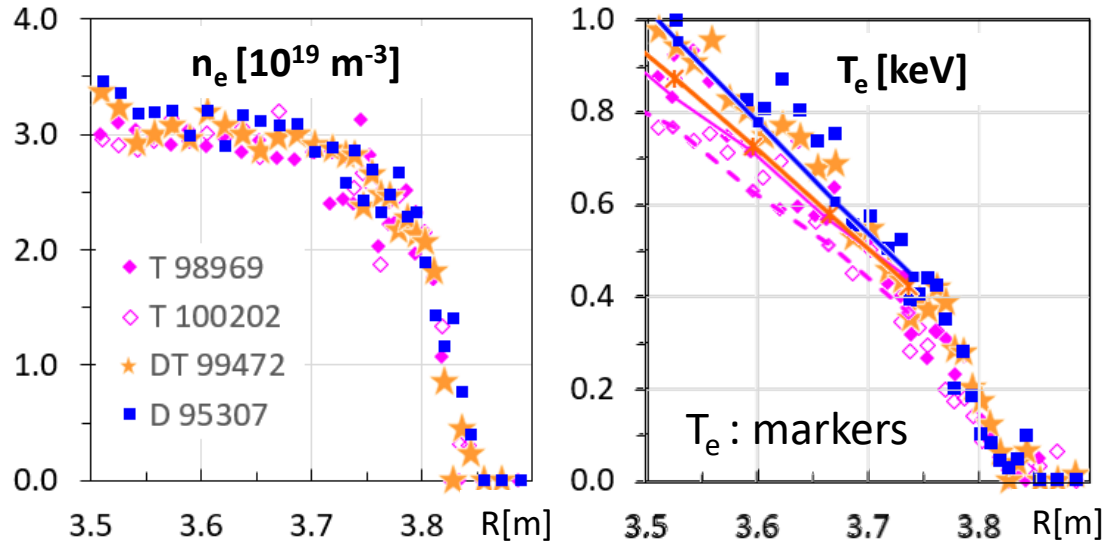
From $r/a=0.5$, very similar n_e , T_e , T_i profiles just before the transition in **D**, **DT**, **T**

ER Solano IAEA FEC 2023

3T 2.5 MA critical profiles



Thomson Scattering < 50 ms before L-H

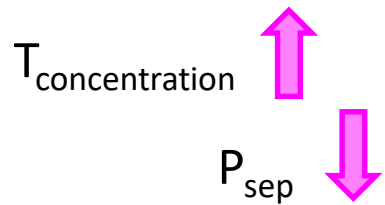
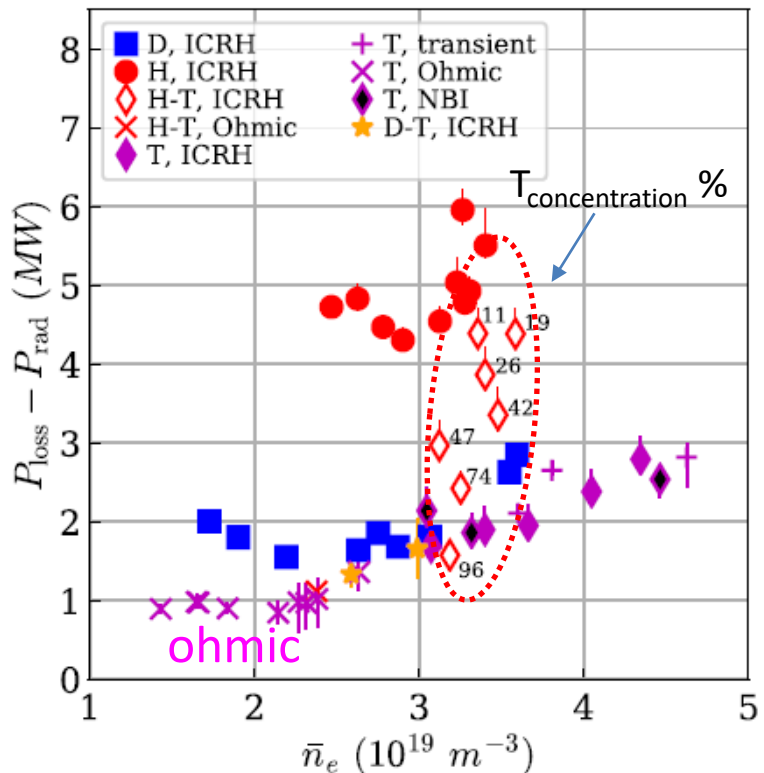


Same profiles at transition require very different P_{LH} depending on plasma isotope:

- T : 3 MW
- DT : 3.2 MW
- D : 5 MW

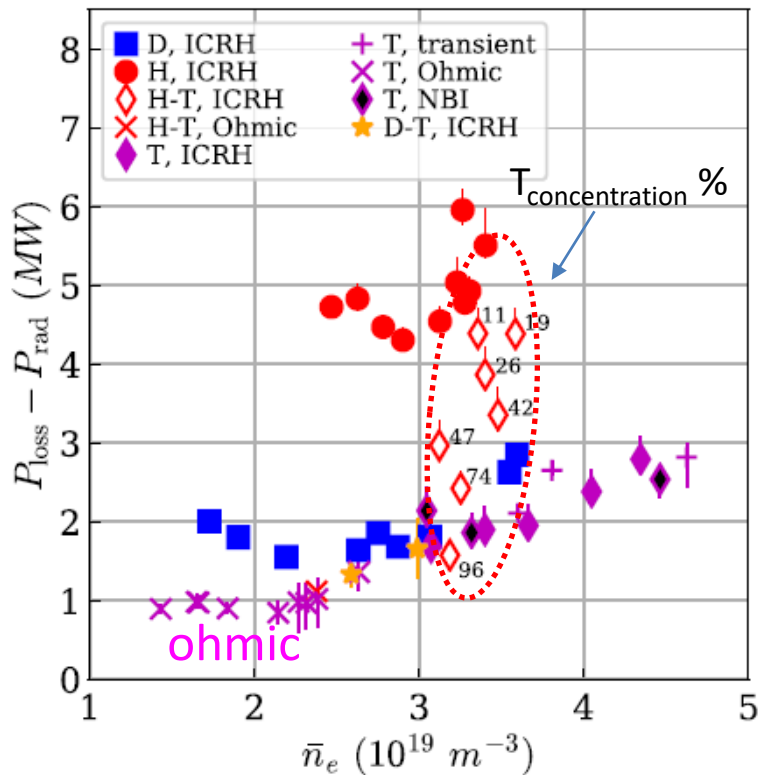
Isotope effect on transition rooted on isotope effect in L-mode

Critical profiles for varying H+T mixtures (1.8T 1.7 MA)



Hydrogen has much higher P_{LH} than Deuterium, larger than Tritium

Critical profiles for varying H+T mixtures (1.8T 1.7 MA)



Isotopic dependency of L-mode transport defines P_{LH}

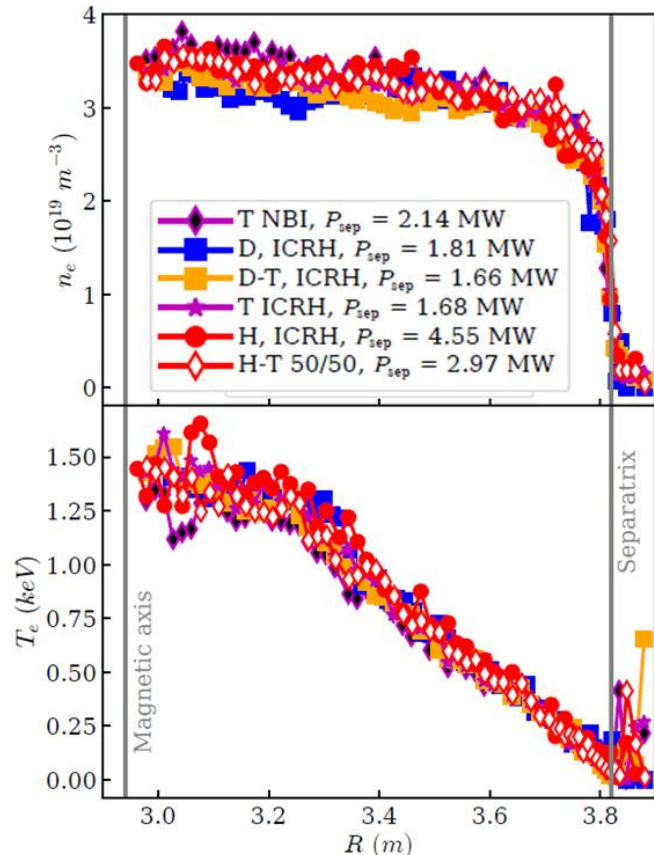


$T_{\text{concentration}}$ ↑
 P_{sep} ↓

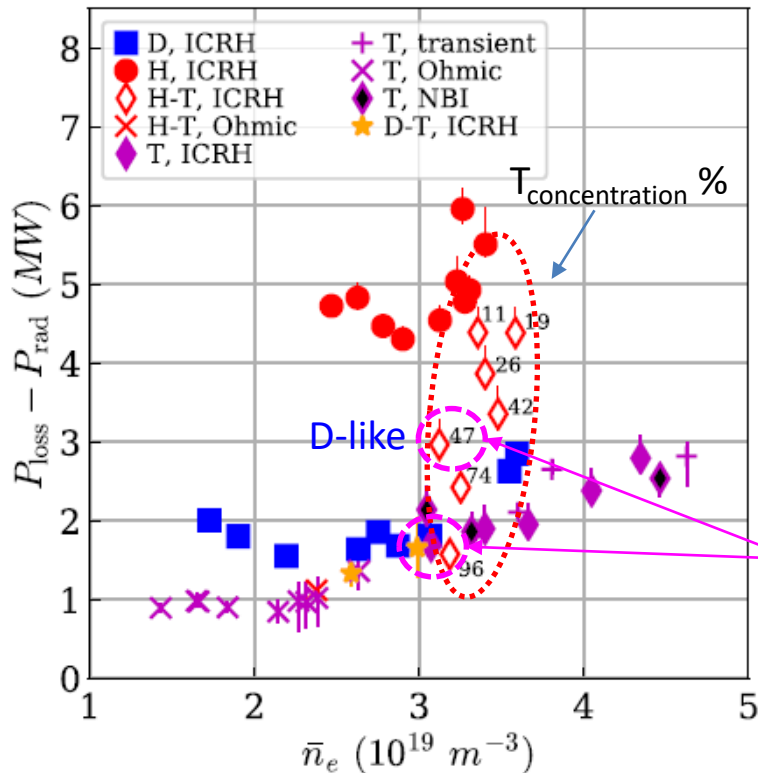
Same critical profiles for all mixtures

Critical profiles?
 Or critical ∇p_e ,
 ∇p_i or ∇p_{total} ?

G. Birkenmeier et al., PPCF (2023)



Critical profiles for varying H+T mixtures



Isotopic dependency of L-mode transport defines P_{LH}



$T_{\text{concentration}}$ ↑

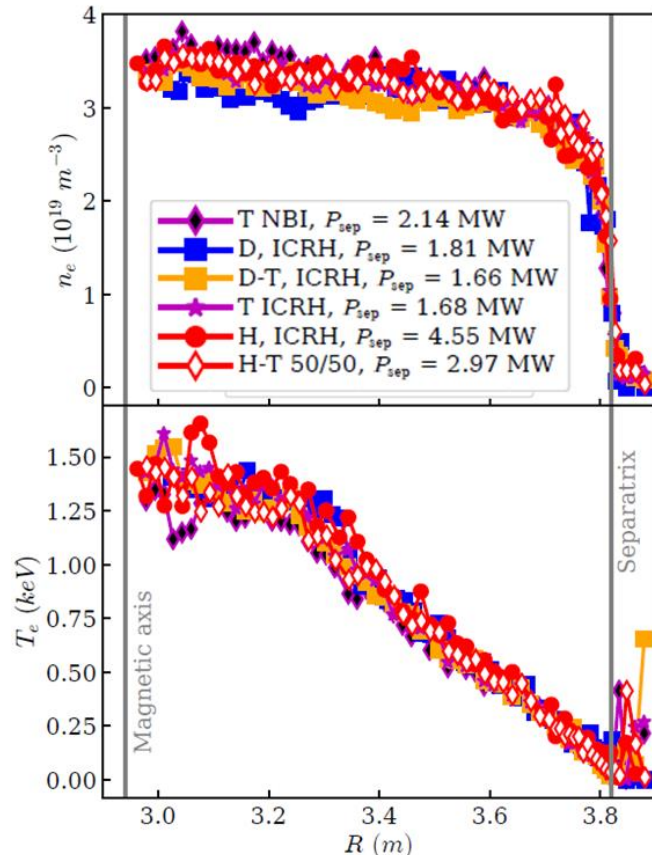
P_{sep} ↓

Same critical profiles for all mixtures

A_{eff} not good!

Critical profiles?
Or critical ∇p_e ,
 ∇p_i or ∇p_{total} ?

G. Birkenmeier et al., PPCF (2023)





Theory?

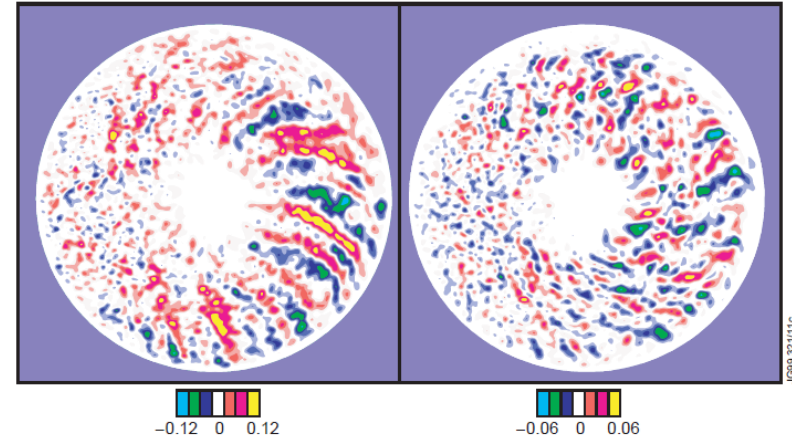
Why does the L-H transition happen?



- In L-mode: turbulence is strong
- In H-mode: turbulence reduced
- The ExB model/paradigm
Sheared ExB rotation breaks up turbulent eddies, reduces turbulent transport
- **Known:** H-mode profiles stabilise turbulence, L-mode profiles don't
- **But L-H transition trigger remains unknown**

Multiple theories develop ExB idea, based on electrostatic turbulence
None succeed in simulating **transition**
consistent with measurements

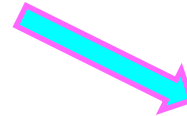
Contour plots of turbulence amplitude, $\frac{e\tilde{\Phi}}{T}$ (simulation)



Without Sheared Flow

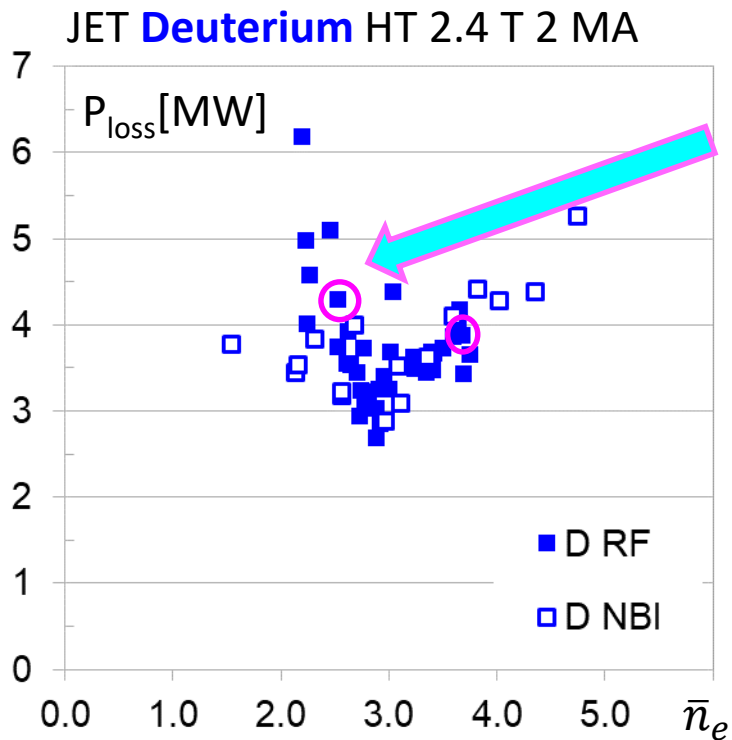
With Sheared Flow

Z. Lin, Science 281,1835(1998)



**Experimental counter-evidence
in Deuterium at JET:
Doppler reflectometry
measurement of v_{\perp}**

Typical results of P_{L-H} density scan in Deuterium



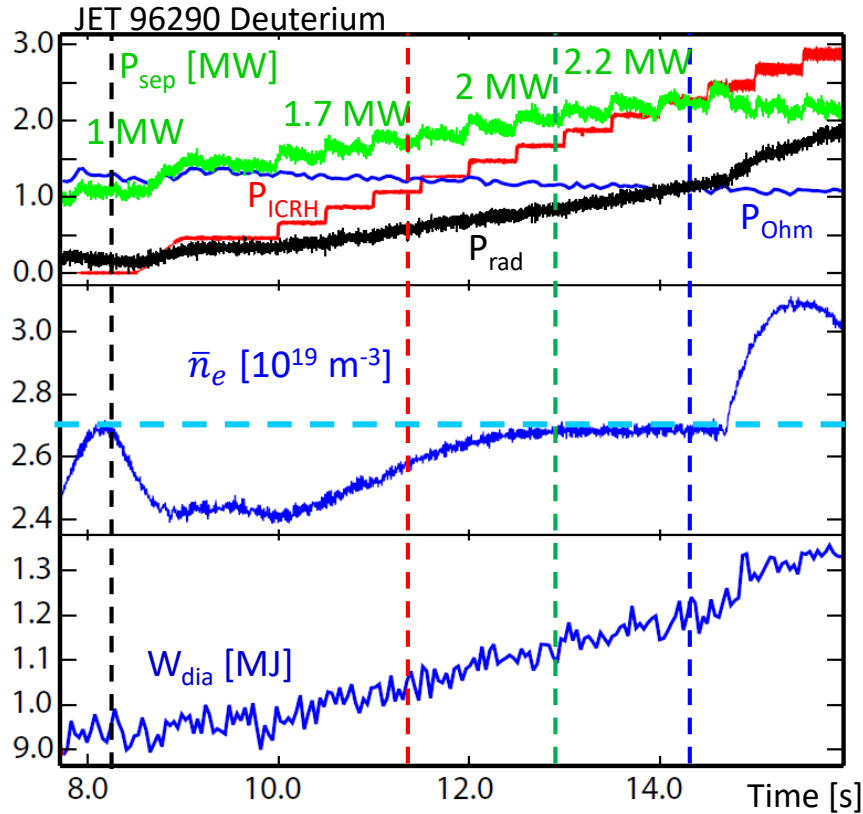
Focus on L-H transition with very detailed Doppler reflectometry measurements

Doppler reflectometry measures v_{\perp} , rotation of fluctuations perpendicular to B

v_{\perp} shear is exactly what will tear or stretch turbulence eddies', if that is the mechanism for L-H transition

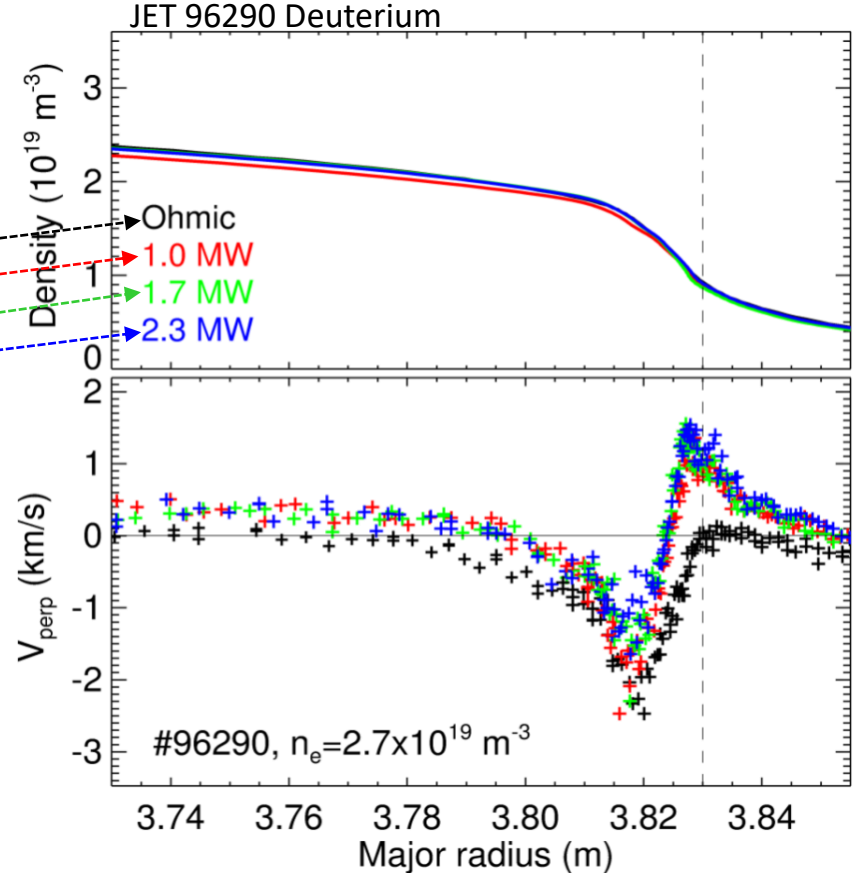
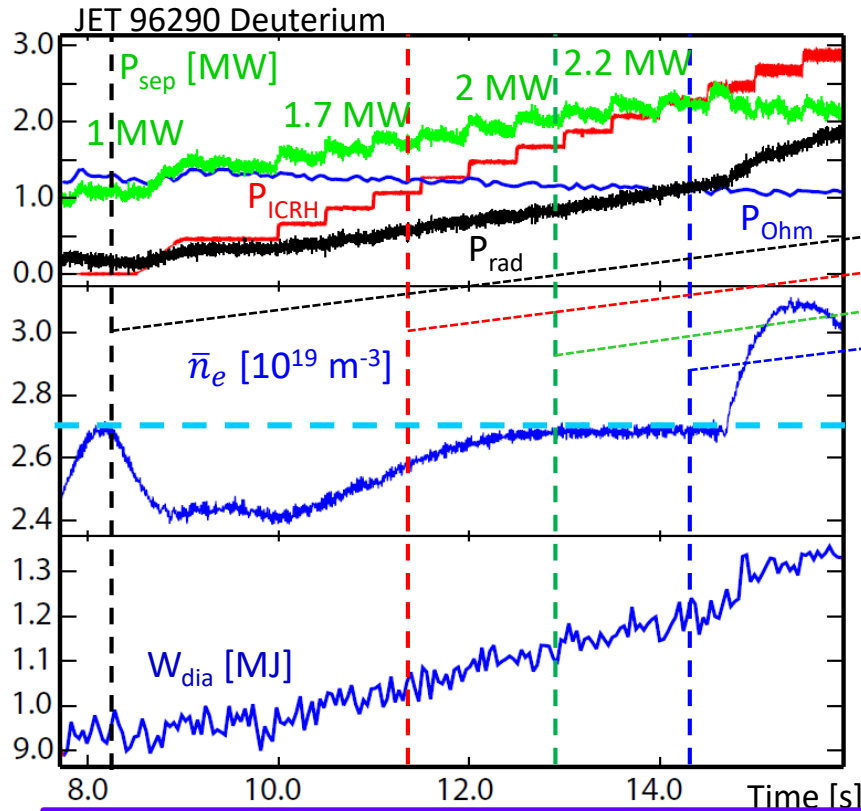
$$v_{\perp} \sim ExB/B^2 \text{ (different from } v_{\text{ion}})$$

Doppler reflectometry along power ramp in Deuterium



C. Silva, Nucl. Fus. 61 126006 (2021)

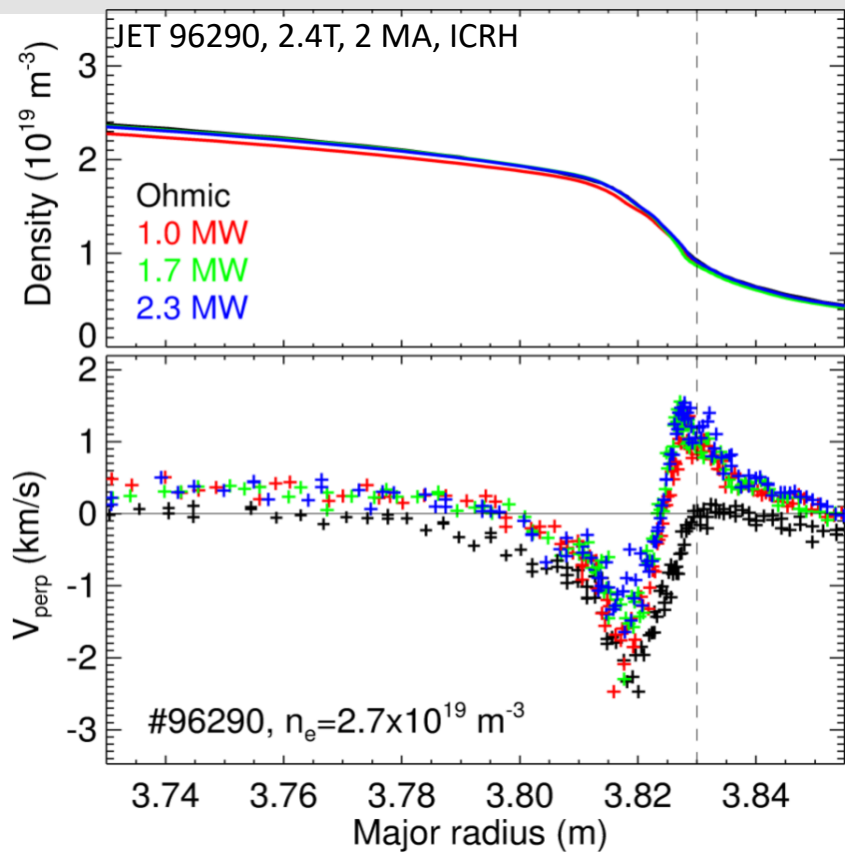
Doppler reflectometry along power ramp in Deuterium



C. Silva, Nucl. Fus. 61 126006 (2021)



Deuterium: E_r measurements along ICRH power ramp, at $n_{e,min}(D)$



Time resolution: 300 ms ($\sim \tau_E$)

No momentum input, RF heating

Ohmic: low v_{\perp} at separatrix/SOL, deep well

During power ramp:

- high v_{\perp} at separatrix/SOL when ICRH on
- reduction in depth of v_{\perp} well with ICRH
- similar v_{\perp} maximum shear during power ramp

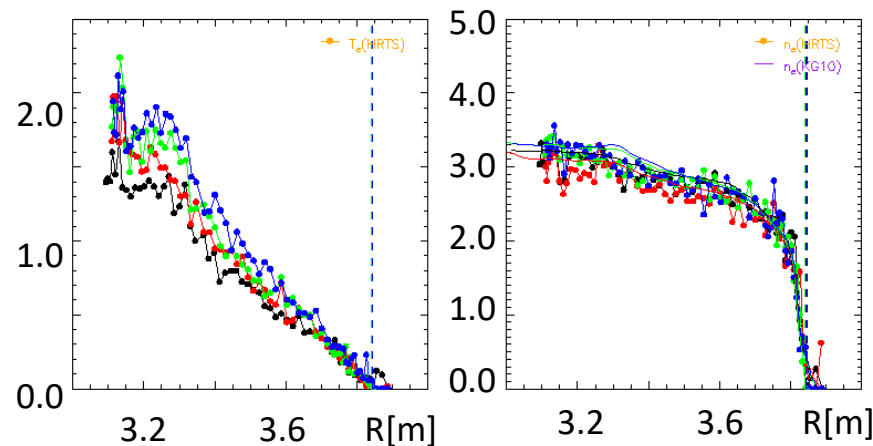
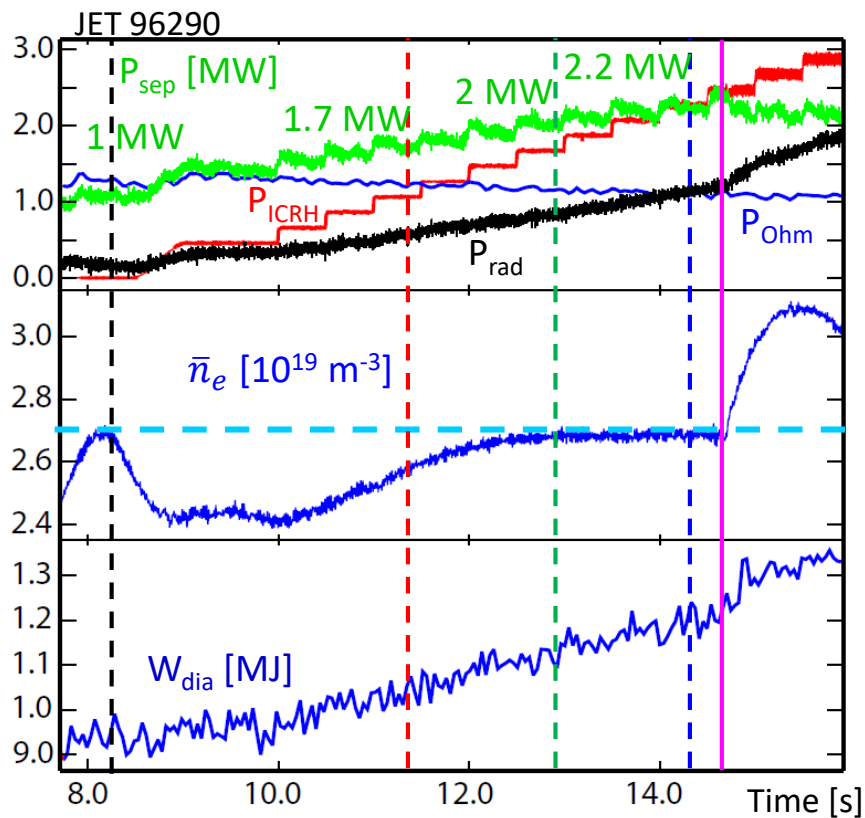
$$\vec{v}_{\perp} = \frac{\vec{E} \times \vec{B}}{B^2} \sim Er/B$$

Neither v_{\perp} well nor v_{\perp} shear increase during the power ramp. No critical E_r well depth
Is this v_{\perp} shape characteristic of L-mode?
If so, what triggers the L-H transition?

C. Silva, Nucl. Fus. 61 126006 (2021)



T_e profile does evolve along the power ramp



- Plasma heated with Ion Cyclotron RF: no T_i or rotation measurements available.
- ∇p does steepen along power ramp.
- Critical ∇p or ∇p_e or ∇p_i ? Not critical E_r .



- Critical profiles n_e , T_e , T_i determine access to L-H transition
- P_{LH} depends on isotope due to L-mode isotopic dependencies
 - L-mode τ_E scaling is VERY old (1989), needs revisiting, especially isotope effect
- Effective mass orders threshold, but not good scaling parameter
- v_{\perp} profile doesn't evolve along power ramp

And what about theory?

Magnetization phase transitions: explored in

Equilibrium criticality when $j_{\theta}=0$: [ER Solano, PPCF 46 L7 \(2004\)](#)

Diamagnetism and ITB formation: [J Garcia, G Giruzzi PRL 104 205003 \(2010\)](#)

Magnetic phase transition, transport barriers: [ER Solano & RD Hazeltine NF 52 114017 \(2012\)](#)

Plasma magnetization in a tokamak

Plasma force balance:

$$\nabla p = \vec{j} \times \vec{B} = \vec{j}_z \times \vec{B}_\theta + \vec{j}_\theta \times \vec{B}_z$$

In cylindrical approximation

$$\frac{d}{dr} \left(p + \frac{B_z^2 + B_\theta^2}{2\mu_0} \right) = -\frac{B_\theta^2}{r\mu_0}$$

$$\frac{dB_z}{dr} = -\mu_0 j_\theta$$

Integrating:

$$\beta_\theta \equiv \frac{\int_0^a p dS}{B_{\theta a}^2 / 2\mu_0} = \frac{B_{za}^2 - \langle B_z^2 \rangle}{B_{\theta a}^2} \simeq 1 + \frac{2B_{za} (B_{za} - \langle B_z \rangle)}{B_{\theta a}^2}$$

β_θ related to volume averaged plasma magnetization

$$\beta_\theta < 1$$

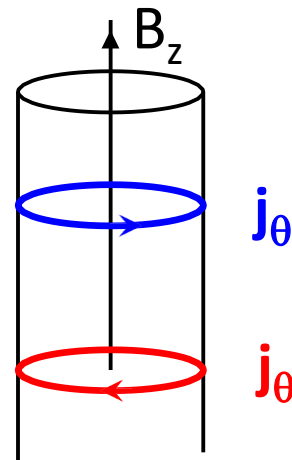
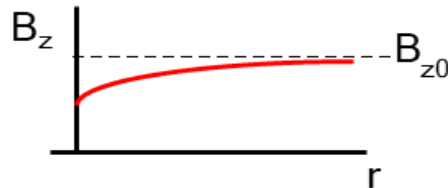
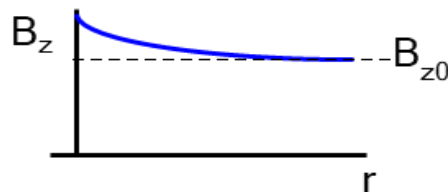
B_z increased by j_θ ,
paramagnetism,
low pressure

$$\nabla p < j_z \times B_\theta$$

$$\beta_\theta > 1$$

B_z reduced by j_θ
diamagnetism,
high pressure

$$\nabla p > j_z \times B_\theta$$



The tokamak plasma is a magnet

Sign of j_θ describes local magnetisation

Magnetisation phase boundary at $j_\theta=0$

Paramagnets

increase the background magnetic field
move towards high field

Diamagnets

increase the background magnetic field
move towards low field

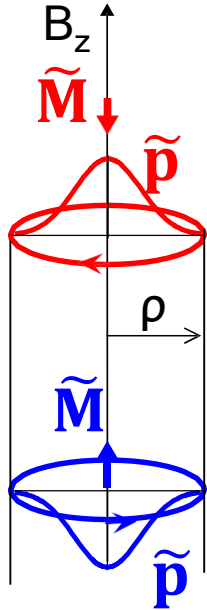


*Diamagnetic frog levitating
in magnetic field*

Berry, Geim (Ig-Nobel)
Eur. J. Phys. **18** 307 1997

Magnetism in cylindrical blob with pressure **peak/hole**

$$\mathbf{F} = mn \frac{d\mathbf{v}}{dt} = -\nabla \tilde{p} + \tilde{\mathbf{j}} \times \mathbf{B} = 0 \quad \tilde{\mathbf{j}}_{\perp} = \frac{\mathbf{b} \times \nabla \tilde{p}}{B}$$



Diamagnetic current: if inside the tube there is a pressure **peak**, the associated \mathbf{j}_{\perp} **reduces** B_z : **diamagnetism**

Paramagnetic current: if inside the tube there is a pressure **hole**, the associated \mathbf{j}_{\perp} **increases** B_z : **paramagnetism**

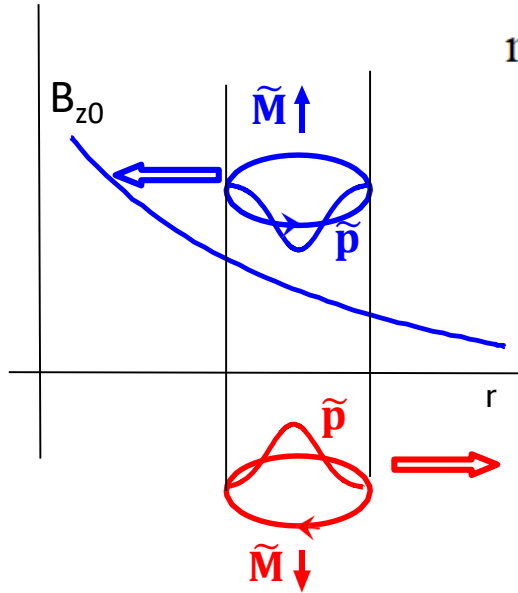
Magnetization of the blob:

$$\nabla \times \mathbf{M} = \mu_0 \frac{\mathbf{b} \times \nabla \tilde{p}}{B} = -\frac{dM}{dr} \hat{\mathbf{r}}$$

$$\tilde{\mathbf{M}} = \frac{1}{\lambda_{\parallel}} \int_0^{\rho} \frac{\mathbf{b}}{B} \frac{\partial \tilde{p}(\rho')}{\partial \rho'} \lambda_{\parallel} d\rho' \approx -\frac{\tilde{p}}{B} \mathbf{b} \quad \left\{ \begin{array}{l} < 0, \text{ dia} \\ > 0, \text{ para} \end{array} \right.$$

Movement of magnetised blobs in paramagnetic plasma

Jackson, Classical Electrodynamics



$$m_V \frac{dv}{dt} \Big|_V = \int (\nabla(\tilde{\mathbf{M}} \cdot \mathbf{B})) dV \underset{\substack{\text{blob magnetization} \\ \boxed{\vec{B} = \vec{B}_0 + \vec{r} \cdot \nabla \vec{B}_0 + \dots}}}{\approx} \left(\int (\vec{r} \times \mathbf{j}_{\text{mag}}) dV \right) \int \nabla B_{0z} dV$$

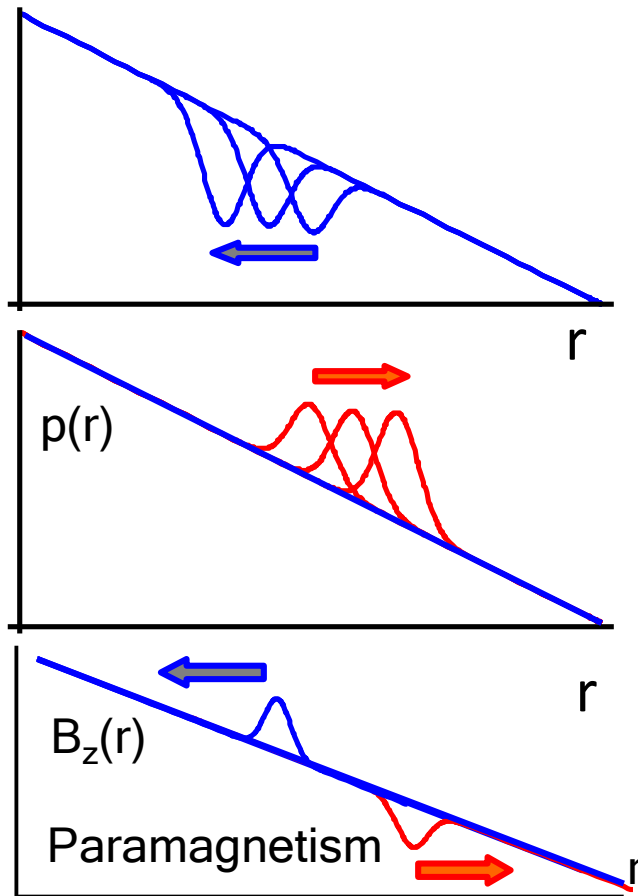
$$m_V \frac{dv_r}{dt} \simeq \tilde{M}_z \nabla \bar{B}_{z0}$$

the **cold blob** (paramagnetic) seeks **high field**

the **hot blob** tube (diamagnetic) seeks **low field**

Blob averaged dB_z/dr controls motion of magnetised plasma
blobs: Anti-potential leads to *magnetic phase separation*

Paramagnetic plasma: L-mode



Motion of pressure blobs depends on dB_z/dr

$$mn_{\nu} \frac{d\vec{v}_r}{dt} \simeq \tilde{M}_{\zeta} \nabla_r \bar{B}_{\zeta 0}$$

paramagnetic cold blobs move inward,
diamagnetic hot blobs move outward

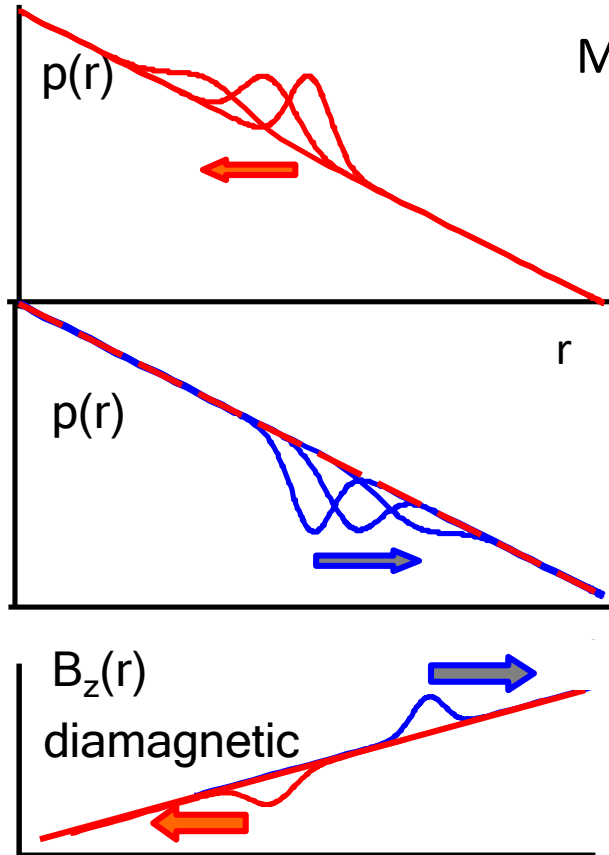
outward thermal energy convection at the
expense of

inward magnetic energy convection

p blobs “grow”, “instability”

L-mode

Diamagnetic plasma: H-mode



Motion of pressure blobs depends on dB_z/dr

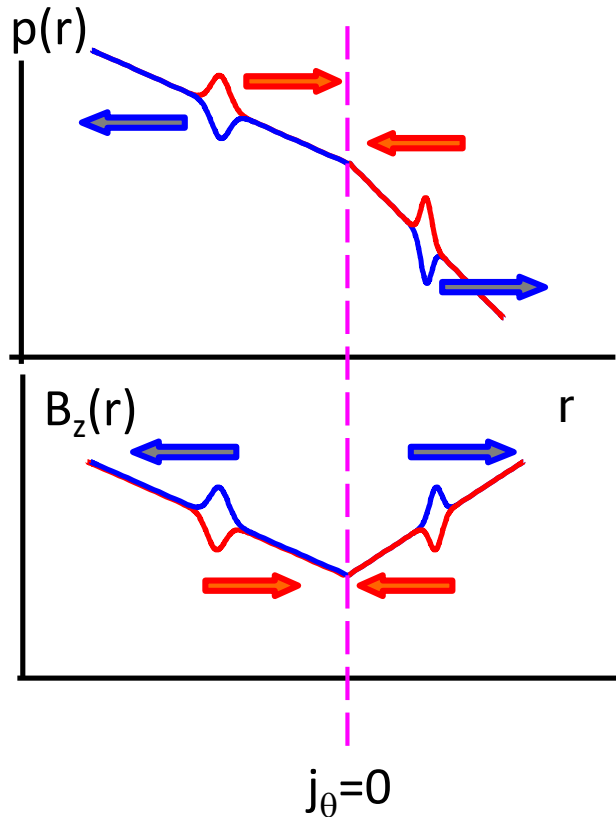
$$mn_{\nu} \frac{d\vec{v}_r}{dt} \simeq \tilde{M}_{\zeta} \nabla_r \bar{B}_{\zeta 0}$$

diamagnetic hot blobs move inward,
paramagnetic cold blobs move outward
inward thermal energy convection
at the expense of
outward magnetic energy convection

p blobs “decrease”, “saturation”

H-mode

Magnetic Boundary: phase transition



At a magnetic phase boundary blobs of the same type accumulate/separate

diamagnetic blobs (heat) seek magnetic wells
paramagnetic blobs seek magnetic hills

With multiple blobs moving,
 p and B_z profiles evolve,
steepening magnetic hills, digging magnetic wells
Developing pressure pedestal

Pedestal formation at magnetisation boundary

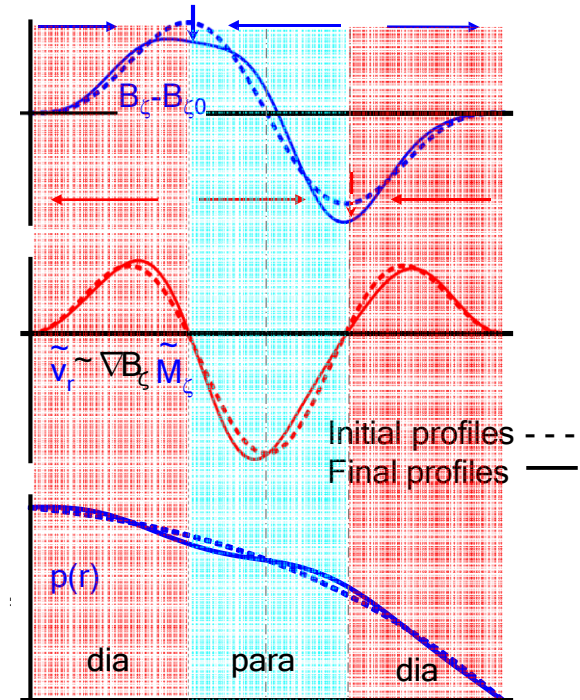
Assume dashed $B_z(r)$, $p(r)$ initial profiles

Ideal MHD with magnetization force

$$\bar{n}_V m_i \left. \frac{d^2 \xi_r}{dt^2} \right|_M = \tilde{M}_\zeta \nabla \bar{B}_{0z}$$

$$\left. \frac{\partial B_z}{\partial t} \right|_M = \nabla \times (\tilde{v}_r \bar{B}_{0z})$$

$$\frac{3}{2} \left. \frac{\partial p}{\partial t} \right|_M = -\nabla(\tilde{p} \tilde{v})$$



Integrating one temporal step

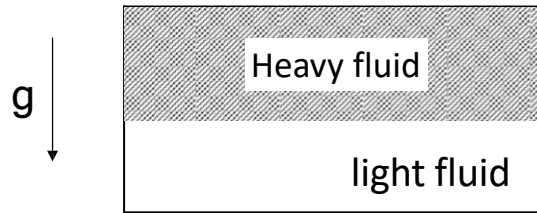
pressure steepens in **diamagnetic** regions, increases **diamagnetism**

flattens in **paramagnetic** regions, increases **paramagnetism**

Magnetic phase separation drives pedestal formation

Interchange instability¹

- present when radial force acts equally on electrons and ions
- equivalent to the Rayleigh-Taylor instability in a fluid.
- magnetization gradient acting on magnetized plasma blobs replace “gravitational field” or “curvature”.



Magnetization interchange

$$\gamma = \sqrt{g\lambda_{\perp}} = \sqrt{-\frac{1}{m_V} \frac{\tilde{p}}{2B^2} \frac{\partial B_{\xi}^2}{\partial r} \lambda_P}$$

Magnetization interchange growth faster for
high magnetisation, blob amplitude & radius, low field & mass

¹M.N. Rosenbluth and C.L. Longmire, Annals of Physics, Volume 1, Issue 2, May 1957,120

Suydam criterion for interchange instability

B. R. Suydam, Proc. 2nd UN Conf. on Peaceful Uses of Atomic Energy, Geneva, 1958.

$$\beta' \left(\frac{Rq}{r_s} \right)^2 \left[\frac{B^2 \kappa_r}{\mu_0} \right] > \frac{q'^2}{4q^2} \quad \text{magnetic shear opposes interchange of tubes driven by cylindrical curvature and } \nabla\beta$$

Generalization: add magnetization force to cylindrical curvature

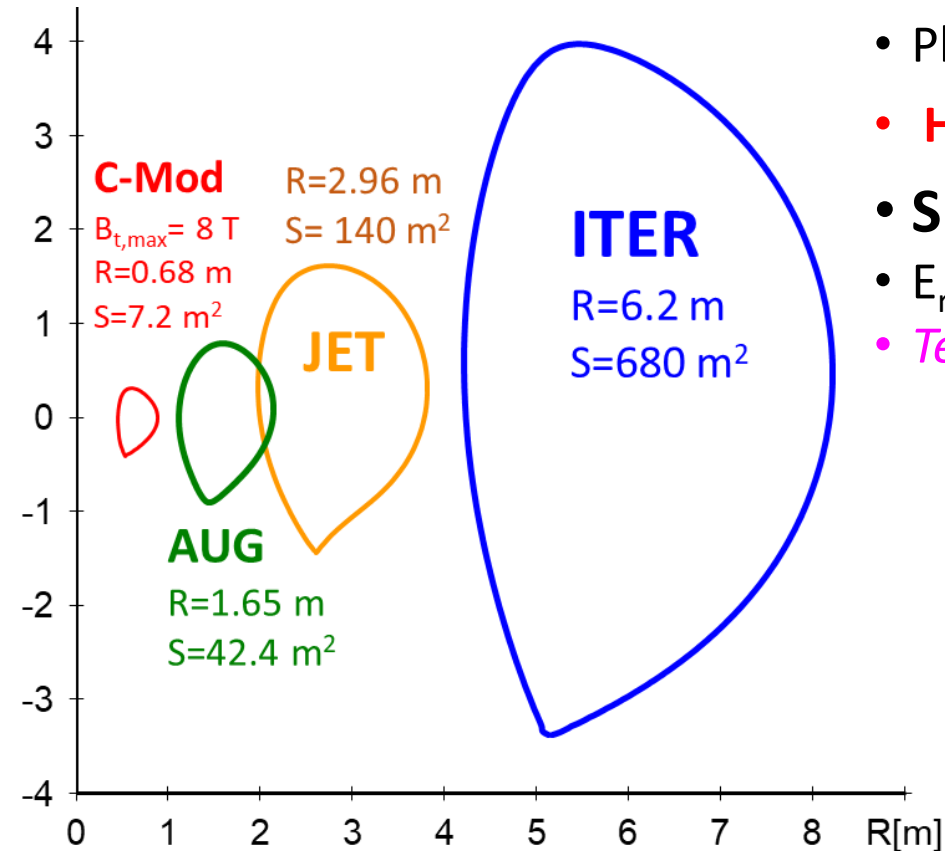
$$\beta' \left(\frac{Rq}{r_s} \right)^2 \left[\frac{B^2 \kappa_r}{\mu_0} + \tilde{M}_z \frac{dB_{0z}}{dr} \right] > \frac{q'^2}{4q^2}$$

In magnetically mixed states $\tilde{M}_z \frac{dB_{0z}}{dr} < 0$

magnetisation force adds to curvature, instability, until the magnetic shear q' or the sign of dB_z/dr changes.

L-H transition power threshold

JET Petition



- Plasma shape affects P_{LH}
- **H**, **D**, **DT**, **T** affects P_{LH}
- **SIZE** and **current** matters
- E_r shear not the only ingredient?
- *Test magnetisation phase transition model?*

Conventional L-H models unlikely to explain our detailed measurements

Much work yet to be done

at JET?

